

BACHELOR OF SCIENCE (B.Sc.)

Term-End Examination

December, 2017

00161

PHYSICS

PHE-11 : MODERN PHYSICS

Time : 2 hours

Maximum Marks : 50

Note : *Attempt all questions. The marks for each question are indicated against it. You may use a calculator or log tables. The values of physical constants are given at the end. Symbols have their usual meanings.*

1. Attempt any **five** parts : **5×2=10**
- (a) Calculate the velocity of an electron when its mass is equal to twice its rest mass.
- (b) Calculate the kinetic energy of an electron whose de Broglie wavelength is 700 nm.
- (c) An electron is confined to a box of length 10^{-8} m. Calculate the minimum uncertainty in its velocity.

- (d) Calculate the expectation value $\langle p_x \rangle$ of the momentum of a particle with the wave function

$$\psi_n(x) = \left(\frac{2}{L}\right)^{1/2} \sin\left(\frac{n\pi x}{L}\right).$$

- (e) The wavelength corresponding to the first transition of Balmer series of hydrogen is 6563 Å. Calculate the wavelength corresponding to the second transition.
- (f) A radioactive element has a half-life of 16 years. Calculate the time in which 70% of the sample will decay.
- (g) Calculate the binding energy per nucleon in ${}_6\text{C}^{12}$.

Given : Mass of ${}_6\text{C}^{12} = 12.0 \text{ u}$

$$m_p = 1.007275 \text{ u}$$

$$m_n = 1.008665 \text{ u}$$

$$m_e = 0.00055 \text{ u}$$

2. Answer any *two* parts :

2×5=10

- (a) Light of wavelength $\lambda = 4850 \text{ \AA}$ is emitted by atoms in a galaxy receding from the earth with a speed of 0.3 c. Calculate the wavelength of light observed on the earth. 5
- (b) Calculate the annual loss in the mass of the sun if approximately 8.4 J of radiated energy is received by each square cm of the earth's surface per minute. The distance of the sun from the earth's surface is $1.15 \times 10^{11} \text{ m}$. 5

- (c) Derive the relation between relativistic energy and momentum of a free particle. 5

3. Attempt any *two* parts : 2×5=10

- (a) What is the probabilistic interpretation of the wave function ? Write down the time dependent Schrödinger equation. Obtain the time independent Schrödinger equation. 1+1+3

- (b) The unnormalised wave function of a particle is given by

$$\phi = Nx \exp\left(-x^2/a^2\right).$$

Determine the normalization constant N. 5

- (c) Show that

$$[L_z, L_x] = i\hbar L_y \quad 5$$

4. Answer any *two* parts : 2×5=10

- (a) Consider a particle of mass m confined in a one-dimensional box :

$$V(x) = 0 \quad -a \leq x \leq a \\ = \infty \quad \text{otherwise}$$

Solve the Schrödinger equation for the particle and obtain its energy eigenvalues. 5

- (b) State Hund's rule. Use Hund's rule to obtain the spectral terms and ground state of Sc ($Z = 21$). 3+2

- (c) X-rays from cobalt ($Z = 27$) tube have a strong K line of wavelength 1.785 \AA and a weak line due to copper impurity ($Z = 29$). Using Moseley's law, calculate the wavelength of the other line. 5

5. Answer any *two* parts : 2×5=10

- (a) Explain the liquid drop model of fission qualitatively with the help of schematic diagrams. 5
- (b) Calculate the distance of closest approach of an α -particle of energy 5.3 MeV fired directly towards a nucleus of gold ($Z = 79$). Given mass of gold nucleus is ($m = 6.7 \times 10^{-27} \text{ kg}$). 5
- (c) List the basic components of a nuclear reactor and explain the functions of moderator and coolant rods. 2+3

Physical Constants :

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$m_p = 1.6725 \times 10^{-27} \text{ kg}$$

$$m_n = 1.6747 \times 10^{-27} \text{ kg}$$

$$c = 3 \times 10^8 \text{ m/s}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\frac{1}{4\pi \epsilon_0} = 9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2}$$